



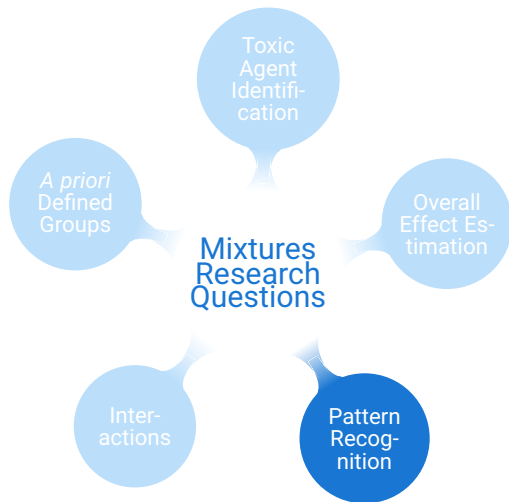
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# Bayesian non-parametric non-negative matrix factorization for identifying patterns in environmental mixtures

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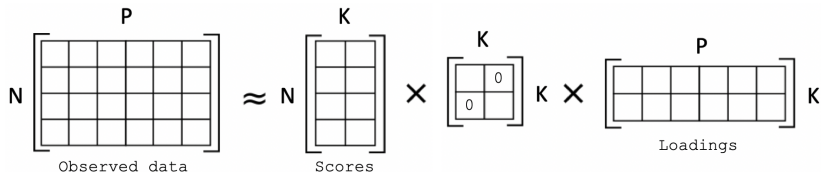
## Existing exposure pattern recognition methods



- Choice of  $k$  patterns subjective
- $+/-$  values not easily interpretable
- Orthogonality constraint not realistic
- No measure of uncertainty

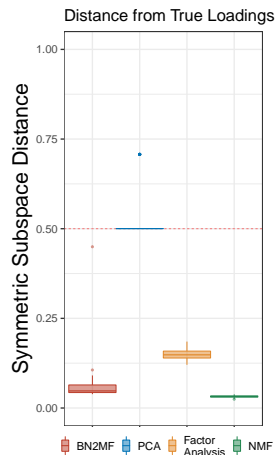
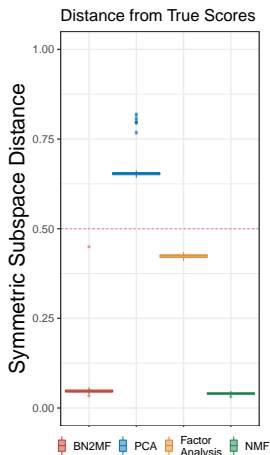
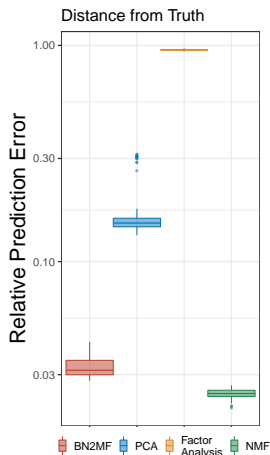
⇒ Proposed solution:

Bayesian non-parametric  
non-negative matrix  
factorization

Bayesian non-parametric non-negative matrix factorization (BN<sup>2</sup>MF)

- ✓ Non-negative continuous Gamma priors
  - ✓ Sparse prior on patterns estimates number
- ✓ No orthogonality constraint
- ✓ Variational confidence intervals

## Results: simulation study



## Conclusion

- Increased interpretability due to:
  - Parts-based (additive) **non-negative** representation of multi-pollutant mixtures
  - Absence of orthogonality constraint on loadings and scores
- ✓ Non-parametric prior on  $k$  helps with model selection
- ✓ Bayesian framework allows uncertainty propagation
- Application to real environmental data can identify sensible patterns

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